

Principles: Qubit



1959, '82 Feynman

"When we get to the very, very small world... We can manufacture in different ways. We can use, not just circuits, but some system involving the quantized energy levels, or the interactions of quantized spins, etc."



Bit

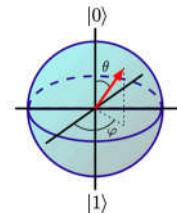
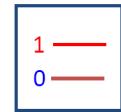
Represent information today

Quantum Bit (Qubit)

Represent information by
two quantum states

0 or 1

$$|\psi\rangle = a|0\rangle + b|1\rangle$$



Vandersypsen, arXiv:0205193v1 (2002)



Principles: Quantum parallelism



Quantum Bit

$$|\psi\rangle = a|0\rangle + b|1\rangle$$



Multiple QuBits

$$|\psi\rangle = |\psi\rangle_1 \otimes |\psi\rangle_2$$

$$|\psi\rangle = a|00\rangle + b|01\rangle + c|10\rangle + d|11\rangle$$



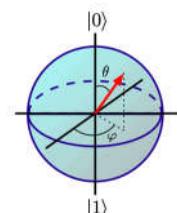
f is a quantum gate

$$a|f(00)\rangle + b|f(01)\rangle + c|f(10)\rangle + d|f(11)\rangle$$

Quantum parallelism: parallel evaluations grow exponentially with the number of Qubits ($\approx 2^n$)



Quantum computation



Vandersypsen, arXiv:0205193v1 (2002)



Principles: Nonlocality, entanglement



Quantum Bit

$$|\psi\rangle = a|0\rangle + b|1\rangle$$

Multiple QuBits

$$|\psi\rangle = |\psi\rangle_1 \otimes |\psi\rangle_2$$

$$|\psi\rangle = b|01\rangle + c|10\rangle$$

f is a quantum gate



$$P_{|1\rangle}^1$$

Projection QuBit 1 to $|1\rangle$

$$a|f(00)\rangle + b|f(01)\rangle + c|f(10)\rangle + d|f(11)\rangle$$

$$|1,0\rangle$$

Quantum parallelism: parallel evaluations grow exponentially with the number of Qubits ($\approx 2^n$)

Nonlocality: manipulation of QBit1 has consequence on QBit2



Vandersypsen, arXiv:0205193v1 (2002)



Parts and Requirements of QC

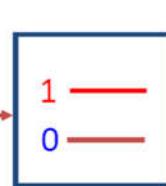
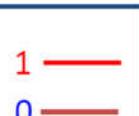


2 level systems:
qubits

Universal set of
unitary gates

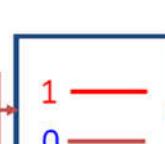
high fidelity
projective readout

coherence

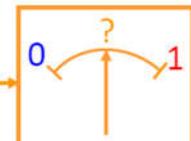


2qubit
Gate

U_2



Readout



efficient reset

"DiVincenzo criteria"



single qubit
Gate



Esteve, Quantum Machines, Les Houches Summer School (2011)

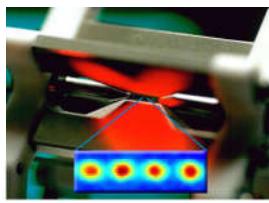
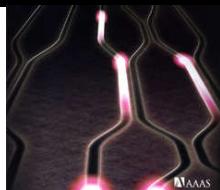
Technologies

Quantum systems with control and manipulation possibility

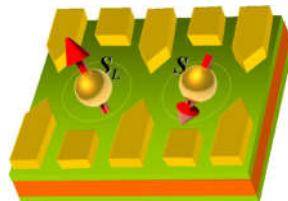
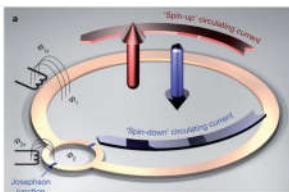
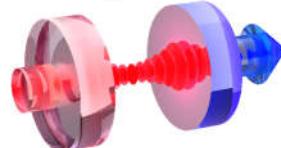
- Photons
- Cavity QED
- Trapped ions
- Superconductors
- NMR
- Quantum dots
- ...

In situ Error corrections!!!

Technology Roadmaps:
US <http://qist.lanl.gov/>,
EU <http://qist.ec.europa.eu/Reports/>



CooPairEnt



Blatt Quantum Machines, Les Houches Summer School (2011)

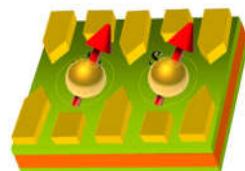


Spin Qubits

CooPairEnt

- Qubit:

$\frac{1}{2}$ spin of single electron trapped into a confinement potential, Scalable system



- Initialization of Qubits

e.g. by B field

- Single Qubit and

by EDSR $T \approx 150\text{ns}$ (2DEG) - 20ns (NW)

- Two-Qubit gates

based on exchange int. $T \approx 200\text{ps}$

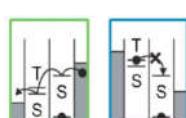
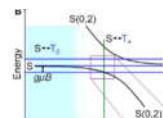
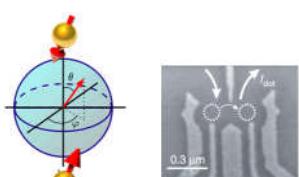
- Readout

Pauli-spin blockade (fidelity >90%)

- Small decoherence

$T_2 \approx 10\text{ns}$, $T_2^* \approx 1\mu\text{s}$

Limited by hyperfine interaction



R. Hanson, Rev Mod Phys, 79, 1217 (2007)

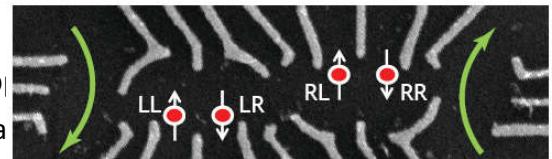


Spin Qubits, Various Material systems



- Qubit:

$\frac{1}{2}$ spin of single electron trapped in a confinement potential, Scale



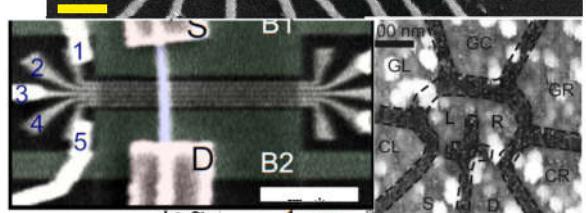
- Initialization of Qubits

- Single Qubit and

Two-Qubit gates

- Readout

- Small decoherence



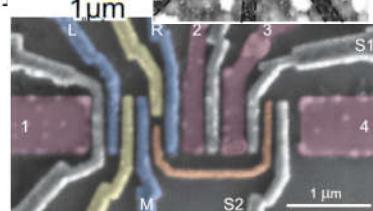
- Nuclear spin free system: C, Si/Ge

- Nuclear polarization

- Faster operation: Singlet-Triplet Qubit

- Topologic protection

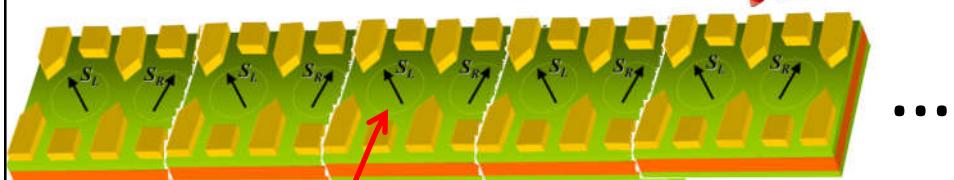
- ...



R. Hanson, Rev Mod Phys, 79, 1217 (2007)



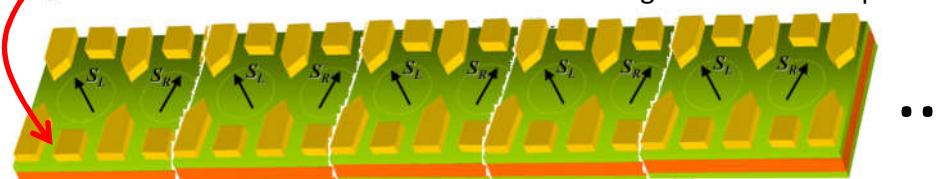
Mobile entangled electrons



1D architecture: interaction only

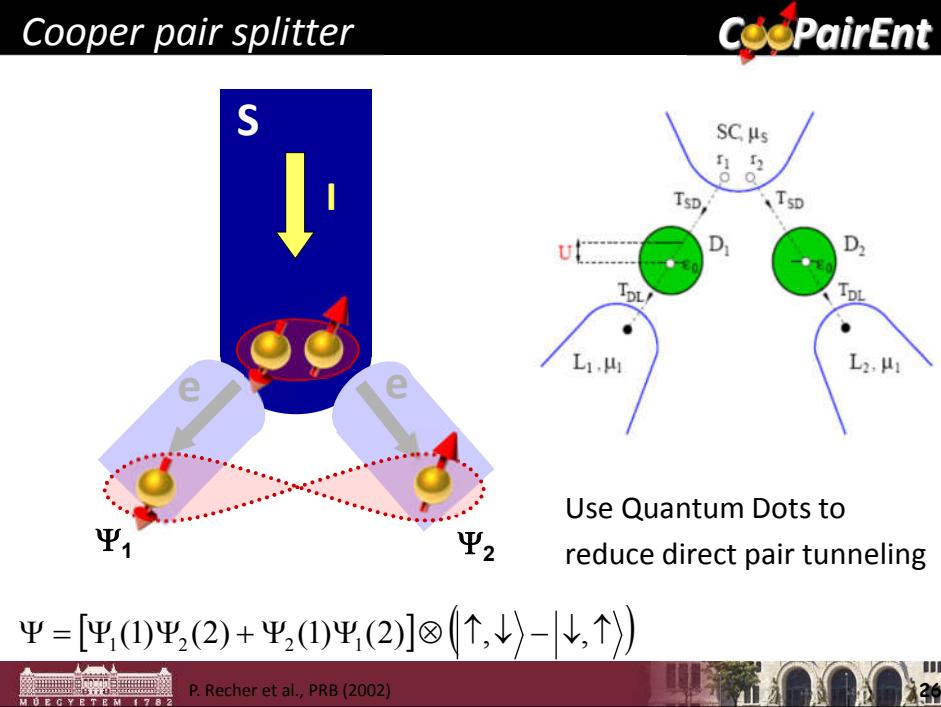
between neighboring qubits

→ Mobile entangled electrons help



R. Hanson, Rev Mod Phys, 79, 1217 (2007)





Atomic scale switches - Memristors

Introduction

- What is a *memristor*? How does it work?
- Applications
- Technology requirements against *real* memory devices

The Ag₂S system

- Experimental technique

Other systems

- Valence change mechanism and versatile switching characteristics in Nb₂O₅

New directions

- Artificial neural networks

A possible realization of resistive switching

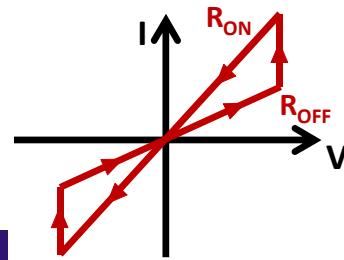
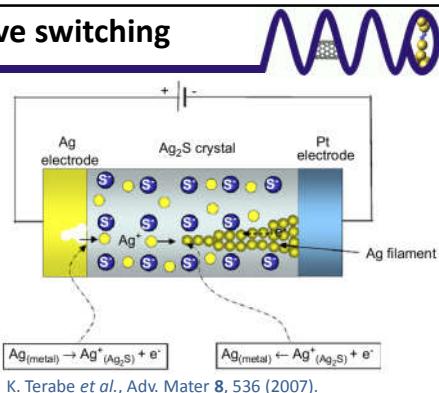
Ag₂S memristor (memory + resistor): Ag electrode + thin Ag₂S layer + electrochemically inert Me tip (e.g. PtIr or Nb).

Positive bias (on the Ag electrode): Ag⁺ ions move towards the Me tip → an Ag filament is grown between the two electrodes → low resistance ON state

Negative bias: the Ag filament is destructed → high resistance OFF state

I(V) characteristics: linear resistive behavior at low bias, switching to ON/OFF state above a positive/negative threshold → ideal for **memory operation**

Resistive Random Access Memory (ReRAM)



Requirements against *real* ReRAM devices

- Write/erase voltage level: < 2 Volt
- Write/erase times: < 100 ns
- Read-out voltage level: < 1 Volt
- Read-out current level: ~ 0.001 – 1 mA
- OFF to ON resistance ratio > 2
- OFF state resistances < 100 kΩ

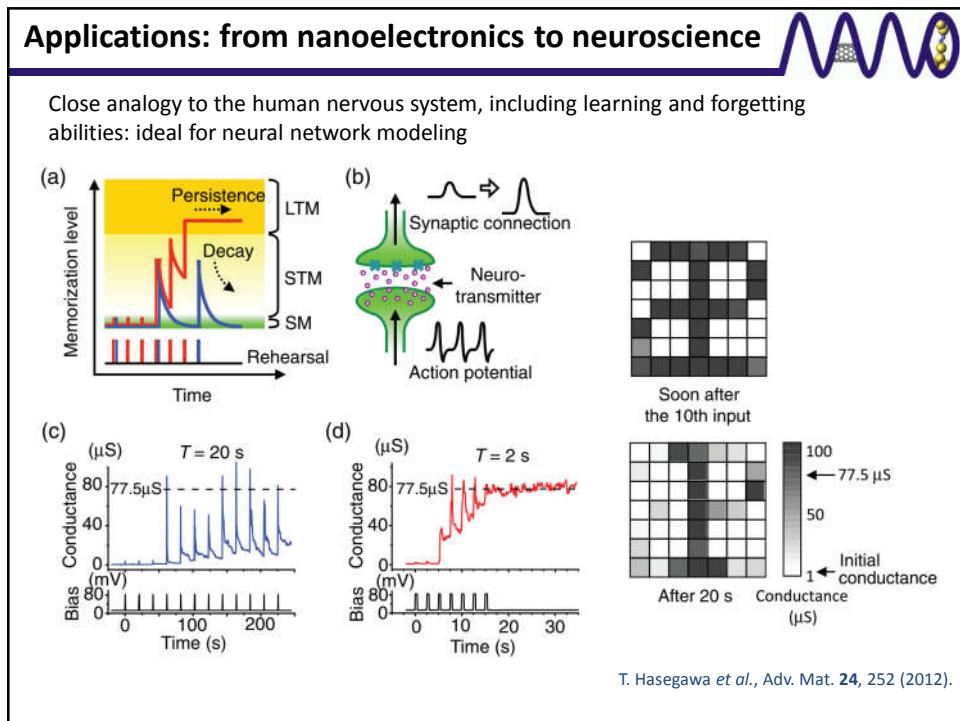
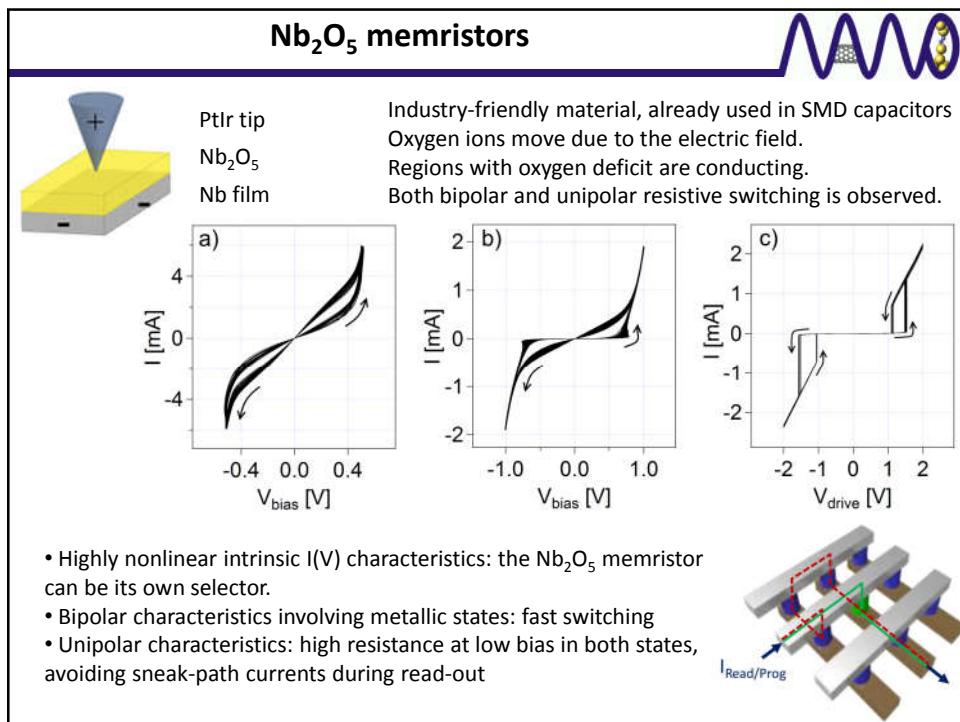
- Endurance > 10⁷ writing cycles
- Retention times > 10 years
- Non-volatility also during read-out operations [R. Waser et al., Adv. Mat. 21, 2632 \(2009\).](#)

[J. J. Yang et al., Nat. Nanotech. 8, 13 \(2013\).](#)

- CMOS competitive scaling
- CMOS compatible material systems and technology

A real resistive memory device must comply to ALL of the above requirements

A highly non-linear voltage response function is essential



Short intro to Spintronics



Outline:

- Motivation of a spin based electronics
- GMR
- Spin injection and detection
- Spin transfer torque
- Spin Hall effect

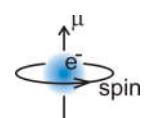
See more:

Halbritter & Csonka: Fundamentals of Nanoelectronics

Motivation



Spin: intrinsic degree of freedom



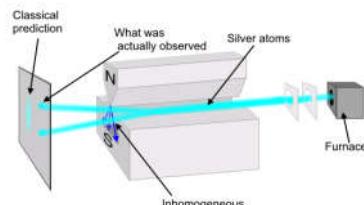
$$\mu_z = -2 \frac{\hbar e}{2m} \sigma_z = -2\mu_B \sigma_z \quad \text{with} \quad \sigma_z = \pm \frac{1}{2}$$

Early studies: Dirac equation



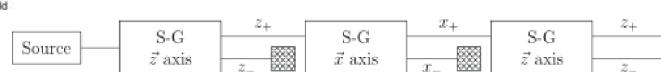
series expansion in the nonrelativistic limit

$$H = H_0 - g\mu_B \vec{\sigma} \vec{B} + \frac{\hbar}{4m^2 c^2} \frac{\partial V_{at}}{\partial r} \vec{p} \vec{\sigma}$$



Spin-magnetic field interaction Spin-orbit interaction

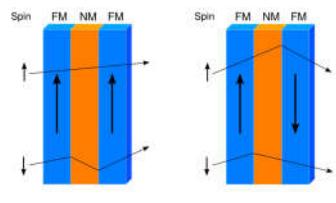
The true quantummechanical nature of the electronspin is demonstrated.



Giant Magnetoresistance

2007

Prototype of spintronic devices



$$\text{Thus: } R_{\uparrow\uparrow} < R_{\uparrow\downarrow}$$

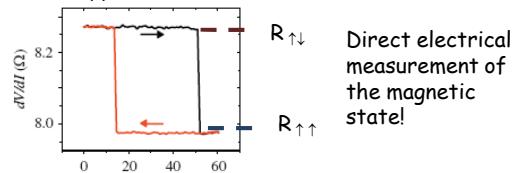
Limits of easy model:

- why only nano?
- role of material parameters
- microscopic description

role of the nonmagnetic spacer: no direct exchange between FM layers

Basic model: two separated current channels for spin up and spin down
Minority spin carriers are scattered due to reduced DOS

Result: increase of resistance for that channel
One layer is denoted free layer, and can be flipped



A. Fert, P. Grünberg

J. F. Gregg, et al, J. Phys. D 35, 121 (2002)

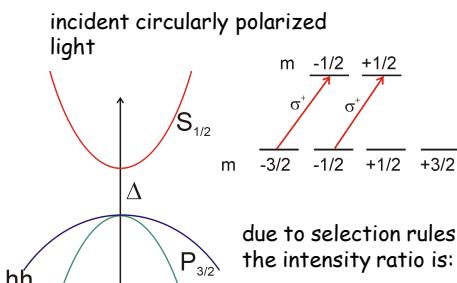
device engineering:

- coercive fields
- FM materials
- FM layer thicknesses
- spacer thickness (RKKY interaction)

Spin injection and detection



Optical pumping/orientation (semiconductors)



due to selection rules the intensity ratio is:

$$\frac{I_{-3/2 \rightarrow -1/2}}{I_{-1/2 \rightarrow +1/2}} = \frac{\left| \langle -3/2, 3/2 | Y_1^1 | 1/2, -1/2 \rangle \right|^2}{\left| \langle -1/2, 3/2 | Y_1^1 | 1/2, +1/2 \rangle \right|^2} = 3$$

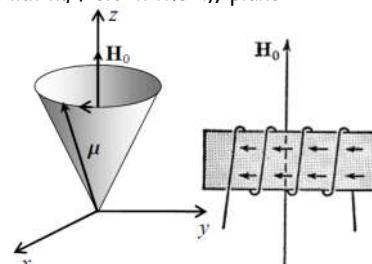
max. value

$$P_{cond} = \frac{n_\uparrow - n_\downarrow}{n_\uparrow + n_\downarrow} \geq \frac{-3 + 1}{3 + 1} = -\frac{1}{2}$$

See more: T. Feher: Group theory,
S. Bordacs Optical spectroscopy

Electron spin resonance:

classical spin precession model:
constant field in z direction, and
oscillating field in the x,y plane



Resonant condition: $\hbar\omega_0 = g\mu_B H$

usually H is swept as the microwave lines are tuned to a specific frequency

T₁ (spin relaxation time)
T₂ (spin dephasing time)

See more: T. Feher: Magnetic resonances

Spin injection and detection

FM-NM interface



current →

Proper handling is

the Valet-Fert

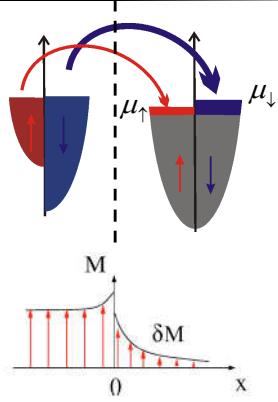
model, i. e.

Boltzmann equation

for two subbands

very low efficiency
for
semiconductors

OK for metals and
graphene



spin imbalance of the current results in a different chemical potential for the two subbands, which decays in bulk

This is detected in the GMR experiment

diffusive spin transport

associated lifetime t_s and length scale l_s

interface spin loss $\delta_{F/N}$

$$\ell_s = \sqrt{D \tau_s} \quad \text{with} \quad \tau_m \ll \tau_s$$

$$D = \frac{1}{3} v_F l_m$$

J. Bass and W. P. Pratt Jr, J. Phys.: Condens. Matter 19, 183201 (2007)

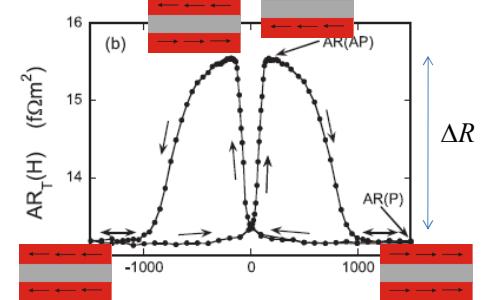
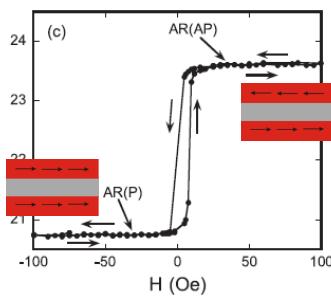
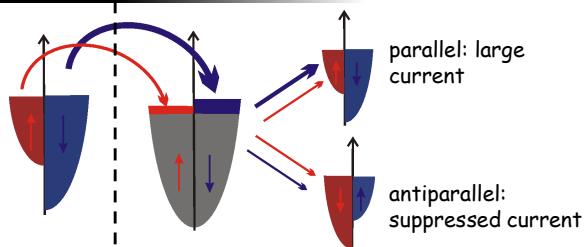
Spin injection and detection

Principle of GMR



current →

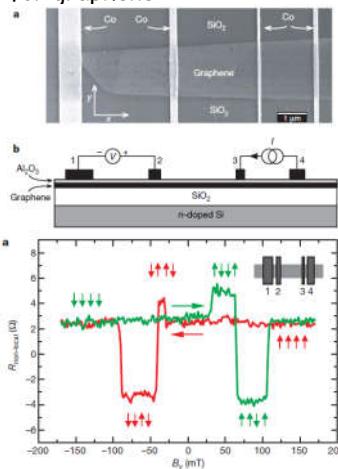
the F layers have different coercive fields (e.g. different layer thickness)



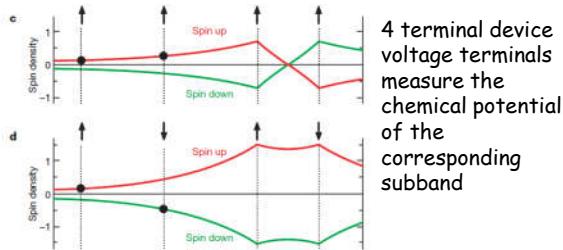
J. Bass and W. P. Pratt Jr, J. Phys.: Condens. Matter 19, 183201 (2007)

Spin injection and detection

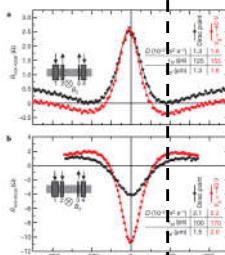
Nonlocal measurements for graphene



Recent measurements spin diffusion length $\sim 10\mu\text{m}$



in a small perpendicular B , precession was also studied (Hanle effect)



in principle: oscillatory behavior

limitations: spin dephasing, diffusive transport

N. Tombros et al, Nature, 448, 571 (2007)

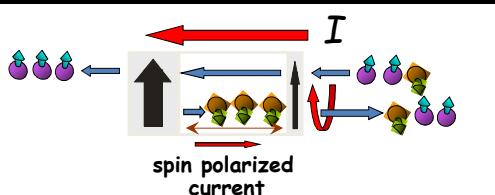
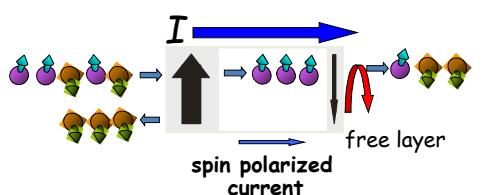


Spin Transfer Torque

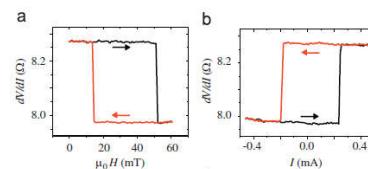
previously: versatile devices, but external magnetic field is necessary to alter spin states. All electric control would be better.



The free layer is rotated by the current instead of the external magnetic field. The shapes are however similar.

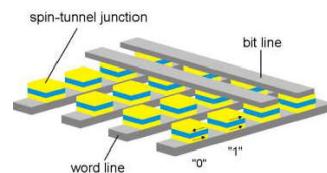


Current density: 10^9 A/cm^2
Only feasible in nano!



Potential application: memory cell

write: STT with high current pulse
read: GMR/TMR at low current

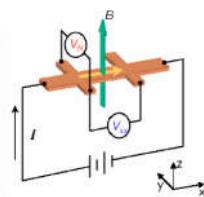


D. C. Ralph and M. D. Stiles, J. of Magn. Mag. Mater. 320, 1190 (2007)

Spin Hall effect



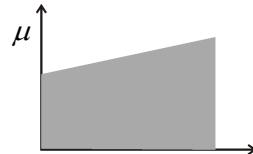
Ordinary Hall effect:



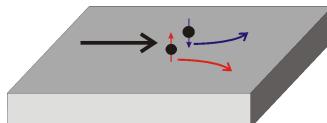
classical model: due to Lorentz force, electrons carrying the current get deflected

$$R_H = \frac{E_y}{j_x B_z} \text{ with } R_H = -\frac{1}{ne}$$

The result is a net electric field in the y direction



If spin-orbit coupling present, momentum scattering becomes anisotropic for each subband



Note: no magnetic field is present!

The generated spin polarization is out-of-plane: $\vec{m} \sim \vec{k}_i \times \vec{k}_f$

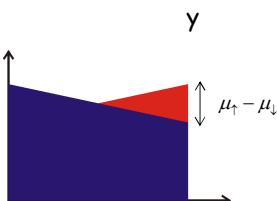
$$V_{SO} = \frac{\hbar}{4m^2 c^2} \frac{\partial V_{at}}{\partial r} \vec{p} \vec{\sigma}$$

No net voltage, only magnetization is visible at the edges

$$m \approx g\mu_B \frac{\partial \rho}{\partial \varepsilon} (\mu_\uparrow - \mu_\downarrow)$$

the device size is limited $l_m < L_y \ll l_s$

J. E. Hirsch, Phys. Rev. Letters, 83, 1834 (1999)



For realistic parameters (Al, 10^6 A/cm²), a small effect is predicted

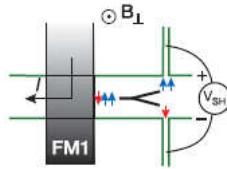
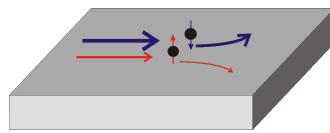
$$\mu_\uparrow - \mu_\downarrow \approx 10 \text{ meV}$$

Spin Hall effect

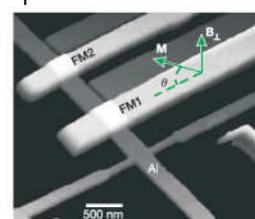


How to measure it?

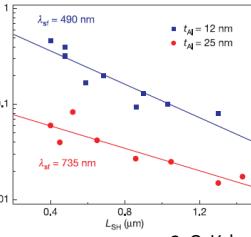
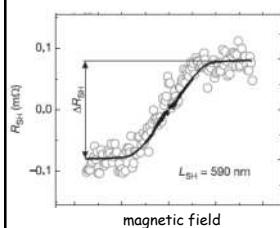
Idea: if the incident current is already spin polarized, then a measurable voltage develops



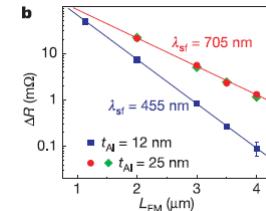
In actual nonlocal experiments, there is no net current through the device, however, the spin imbalance develops



Out-of-plane magnetic field is necessary to have such magnetization to generate a signal



the device is characterized using FM2 in a standard nonlocal measurement



S. O. Valenzuela and M. Tinkham, Nature, 442, 176 (2006)

Literature



Prepared by A. Geresdi

Basics:

- I. Zutic, J. Fabian and S. Das Sarma, *Rev. Mod. Phys.*, 76, 323 (2004)
J. F. Gregg, I. Petej, E. Jouguet and C. Dennis, *J. Phys. D* 35, 121 (2002)
M. N. Baibich, J. M. Broto, A. Fert, F. Nguyen Van Dau, F. Petroff, *Phys. Rev. Letters*, 61, 2472 (1988)
Cserti József, *Természet Világa* 2005/9. 386

Wikipedia

ESR:

Fehér Titusz, ESR mérésleírás (2010)

Dario Quintavalle, PhD thesis (2008)

GMR in CPP geometry, spin diffusion length:

- J. Bass and W. P. Pratt Jr, *J. Phys.: Condens. Matter* 19, 183201 (2007)
H. Kurt, R. Loloee, K. Eid, W. P. Pratt, Jr., and J. Bassa, *Appl. Phys. Letters*, 81, 4787 (2002)
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